Grade 8 Math: Final Exam Review

Unit 5: Percent, Ratio and Rate

Lesson 5.1: Relating Fractions, Decimals and Percents

1. Write each percent as a fraction and as a decimal.

a) 24.5%

b) $2\frac{4}{5}\%$

c) 73.25%

d) $99\frac{3}{4}\%$

2. Use a hundredths chart to represent 1%.

Shade the chart to represent each percent.

a) 0.3%

b) 0.55%

c) 0.04%

d) 0.9%

e) 0.335%

f) 0.5525%

g) 0.0475%

h) $\frac{1}{5}\%$

3. Write each fraction as a decimal and as a percent.

a) $\frac{5}{200}$

b) $\frac{3}{150}$

c) $\frac{12}{500}$

d) $\frac{9}{300}$

e) $\frac{16}{400}$

f) $\frac{12}{250}$

g) $\frac{15}{600}$

h) $\frac{28}{800}$

4. Write each percent as a fraction and as a decimal.

a) 0.7%

b) 0.44%

c) 0.15%

d) 0.9%

e) 0.92%

f) 0.27%

g) 0.55%

h) 0.36%

5. Write each decimal as a fraction and as a percent.

a) 0.221

b) 0.003

c) 0.2225

d) 0.0095

e) 0.016

f) 0.375

g) 0.1875

h) 0.0031

6. Elaine scored 19 out of 24 on her science test.

Addison had 81.25% on the same test.

Who did better?

How do you know?

7. During a school tournament, Team A had 10 of its 12 team members present.

Team B had 13 of its 15 players present.

Which team had the lesser percent of its team present at the tournament?

Lesson 5.2: Calculating Percents

1. Write each percent as a decimal.

Draw a diagram or number line to illustrate each answer.

a) 275%

b) 156%

c) 320%

d) 0.25%

e) 0.5%

f) 0.58%

2. Write each fraction as a percent.

Draw diagrams to illustrate your answers.

a) $\frac{6}{5}$

b) $\frac{45}{40}$

- **c**) $\frac{15}{3}$
- **d**) $\frac{9}{6}$
- **e**) $\frac{60}{25}$
- **f**)
- **3.** a) Find each percent of the number.

Draw a diagram to illustrate each answer.

- **i)** 400% of 240
- **ii)** 40% of 240
- **iii)** 4% of 240
- iv) 0.4% of 240
- **b)** What patterns do you see in your answers in part a?
- c) Use the patterns in part a to find each percent.
 - i) 4000% of 240
- ii) 0.04% of 240
- **4.** One hundred sixty students attended Music Night on Thursday night.

The attendance on Friday night was 120% of the attendance on Thursday night.

The attendance on Saturday night was 75% of the attendance on Friday night.

- a) How many people attended Music Night on Friday night?
- **b)** How many people attended on Saturday night?
- c) What was the total attendance for the 3 nights?
- **5.** A house was purchased for \$450 000.

Three years later, the house was sold for 124% of its purchase price.

- a) What was the selling price of the house?
- **b)** Estimate to check your answer.
- c) By how much did the value of the house increase over the three years?
- **6.** In a 500-word assignment, the teacher noted that 1.2% of the words were incorrectly spelled.
 - a) How many words were correctly spelled?
 - **b)** Estimate to check your answer.

Lesson 5.3: Solving Percent Problems

- 1. Find the number in each case.
 - **a)** 30% of a number is 12.
 - **b)** 2% of a number is 9.
 - **c)** 150% of a number is 60.
 - **d)** 55% of a number is 11.

- **2.** Find the whole amount in each case.
 - **a)** 8% is 72 cm.
 - **b**) 0.6% is 18 g.
 - c) 120% is 24 m.
 - **d)** 32% is 64 mL.
- **3.** Write each increase as a percent.
 - a) The price of gasoline increased from 93.9¢ to 99.9¢.
 - **b)** The price of a car increased from \$32,000 to \$36,000.
 - c) The price of a loaf of bread increased from \$1.99 to \$2.49.
- **4.** Write each decrease as a percent.
 - a) The number of employees decreased from 6800 to 5200.
 - **b)** The area of a park decreased from 840 ha to 672 ha.
 - c) The price of a computer decreased from \$1500 to \$1200.
- **5.** A printing machine produces labels.

Four percent of the labels produced are defective.

Suppose 372 labels were defective.

How many labels are not defective?

6. A field goal kicker was successful 75% of the time.

He made 51 field goals.

How many kicks did he make in total?

7. Lesley and Enid left their waitress a 15% tip.

The tip was \$10.25.

What was their total bill, not including the tip?

8. Marcus collects baseball cards. At the end of 2005, he had 250 cards.

His collection increased by 12% in 2006, and by 15% in 2007.

- a) How many baseball cards did Marcus have at the end of 2007?
- **b)** Is your answer to part a the same as a 27% increase in the number of cards Marcus had at the end of 2005? Why or why not?

Lesson 5.4: Sales Tax and Discount

- 1. Suppose you are in Prince Albert, Saskatchewan.
 - a) Find the sales taxes on each item.
 - **b)** Calculate the selling price, including taxes.
 - i) a pair of running shoes that costs \$89.60
 - ii) a box of golf balls that costs \$24.86

2. The regular price of a skateboard is \$74.99.

Find the sale price when the skateboard is reduced by:

a) 30%

b) 25%

c) 60%

d) 50%

Calculate each sale price, including taxes of 13%.

3. Suppose you are in Watson Lake, Yukon.

For each item below:

- a) Calculate the discount.
- **b**) Calculate the sale price, before taxes.
- c) Calculate the sale price, including taxes.
 - i) Notebook computer: Regular price \$1598, now 20% off
 - ii) Digital camera phone: Regular price \$158, now 15% off
- **4.** Suppose you are in Port Moody, British Columbia.

For each item below, calculate:

- i) the percent decrease in price
- ii) the sale price, including taxes
 - a) a television marked down from \$1488 to \$1100
 - b) an electronic game marked down from \$56.84 to \$49.99
- 5. A camera shop in Lloydminster, Alberta, reduced the price of a digital camera by 10% at the end of the first week, by 20% at the end of the second week, and by a further 20% at the end of the third week. The original price of the camera was \$625.
 - a) Calculate the sale price after 3 weeks.
 - **b)** Calculate the sale price, including the sales taxes.
- **6.** During a 15% off sale, the sale price of a garden bench was \$84.99.

What was the regular price of the bench?

7. A furniture store offers two choices of discount on a sofa with a price of \$1250.

Choice A: 15% discount Choice B: \$200 rebate

Which is the better deal for the customer?

Justify your answer.

Lesson 5.5: Exploring Ratios

- 1. A baseball team has 3 outfielders, 4 infielders, and a battery (the pitcher and the catcher). Write each ratio.
 - a) outfielders to infielders
 - **b)** infielders to the battery
 - c) the battery to the entire team

- **2.** Write each ratio in two different ways.
 - a) a tricycle's wheels to a bicycle's wheels
 - **b)** a tricycle's wheels to a car's wheels
 - c) a tricycle's wheels to a car's wheels to a bicycle's wheels
 - d) a tricycle's wheels to a bicycle's and a car's wheels
- **3.** There are 7 cows and 5 chickens in a farmer's field.
 - a) Write the ratio of cows to all the animals in the field.
 - **b)** Write the ratio in part a as a percent.
- **4. a)** Draw two different diagrams to show the ratio 2:3.
 - **b)** Draw a diagram to show the ratio 5:3.
 - c) Draw a diagram to show the ratio 4:3:5.
- **5. a)** Write a part-to-part ratio to compare the items in each sentence.
 - i) A student has 3 red pens, 2 black pens, and 7 blue pens.
 - ii) On the chess team, there are 4 girls and 3 boys.
 - iii) A box contains 8 apple-flavoured granola bars and 4 oatmeal-flavoured granola bars.
 - **b)** Write a part-to-whole ratio for the items in each sentence in part a. Express each ratio as many ways as you can.
- **6.** A bag contains 4 strawberry, 3 grape, 2 orange, 5 raspberry, and 6 cherry gumballs.
 - a) Write each ratio.
 - i) strawberry:cherry
 - ii) grape:raspberry
 - iii) raspberry:strawberry:cherry
 - iv) orange and cherry: all the gumballs
 - **b)** Suppose 1 grape, 2 raspberry, and 3 cherry gumballs were eaten. Write the new ratios for part a.
- 7. a) How could you explain 3:4 as a part-to-part ratio?
 - **b)** How could you explain 3:4 as a part-to-whole ratio?

Lesson 5.6: Equivalent Ratios

- **1.** Write 3 ratios equivalent to each ratio.
 - **a**) 4:5
- **b**) 18:12
- **c**) 7:2
- **d**) 50:10

- **e)** 18:3
- **f**) 4:9:10
- **g**) 2:7:4
- **h**) 12:3:9

- **2.** Write each ratio in simplest form.
 - **a)** 6:18
- **b**) 10:25
- c) 16:12:20
- **d**) 15:60:45

3. Find pairs of equivalent ratios. How do you know they are equivalent?

 3:15:21
 3:6

 2:7
 9:18

 2:5
 12:15:21

 20:50
 8:28

 10:18
 2:10:14

 24:30:42
 5:9

- **4.** Write a ratio, in simplest form, to compare the items in each sentence.
 - a) On the bus, there are 14 girls and 12 boys.
 - **b)** In the garden, there are 12 rose bushes and 4 lilac bushes.
 - **c**) On the bookshelf, there are 7 mystery books, 28 non-fiction books, and 21 science-fiction books.
 - **d**) In a parking lot, there were 6 American cars, 12 Japanese cars, and 9 Korean cars.
- 5. How many equivalent ratios are there for 3:4 in which the sum of all the digits is less than 10? Write the ratios you find.
- **6.** Use the ratios below.

A	***	***
В	^	* * *
С	***	***
D	>>	00000

- a) Use the ratios in row A.
 - If there are 16 clubs, how many hearts are there?
- **b)** Use the ratios in row B.
 - If there are 24 diamonds, how many spades are there?
- c) Use the ratios in row C.
 - If there are 2 diamonds, how many arrows are there?
- **d)** Use the ratios in row D.
 - If there are 4 squares, how many arrows are there?

Lesson 5.7: Comparing Ratios

- **1.** Write each ratio with first term 1.
 - a) 6:18
- **b**) 36:108
- **c)** 9:63
- **d**) 10:110
- **2.** Write each ratio with second term 1.
 - **a)** 119:17
- **b)** 156:26
- **c)** 72:12
- **d)** 160:20

3. Mr. James' class has a ratio of 2 boys to 3 girls.

Ms. Singh's class has a ratio of 1 girl to 2 boys.

Both classes have 30 students.

How many boys and girls are in each class?

4. At the carnival, the Ring Toss advertises that 3 of every 7 players win a prize.

The Pop the Balloon game advertises that 4 of every 9 players win a prize.

Which game would you play? Explain.

5. The Blazers hockey team has won 7 of its first 12 games.

No game was tied.

The Rockets' record is 5 wins and 3 losses.

Which team has the better record?

6. Concentrate and water are mixed to make juice.

Which is the stronger mixture: A or B? Explain.

Mixture A: 3 parts concentrate to 5 parts water

Mixture B: 4 parts concentrate to 7 parts water

7. Here are the ratios of cats to dogs in different kennels in the city.

In each case, state which kennel has the greater number of dogs.

- a) Kennel A, 5:6 or Kennel B, 7:9
- **b**) Kennel C, 8:11 or Kennel D, 15:19
- c) Kennel E, 3:4 or Kennel F, 2:3
- **8.** There is a total of 600 blue, yellow, and red balls in a machine.

The ratio of blue balls to the total number of balls is 1:4.

The ratio of yellow balls to blue balls is 7:3.

The ratio of blue balls to red balls is 3:2.

Which colour of balls is most common?

Lesson 5.8: Solving Ratio Problems

- 1. Find the value of each variable.
 - **a)** x:8 = 9:24
- **b**) y:15 = 7:3
- c) a:8 = 9:4
- **d**) p:12 = 15:10
- **e**) b:5 = 18:6 **g**) 2:7 = 20:d
- **f**) t:11 = 6:33**h**) 34:85 = f:5
- i) 45:30 = 6:s
- \mathbf{j}) 9:36 = c:8
- **2.** An advertisement claims that 7 out of 8 people prefer Brand X.

Suppose 216 people were interviewed.

Find the number of people who prefer Brand X.

3. The Grade 8 students held a graduation dance.

Four out of 7 students attended.

There are 112 Grade 8 students.

How many students attended the dance?

4. A ski shop rents 5 snowboards for every 3 sets of skis it rents.

Suppose 126 sets of skis were rented.

How many snowboards were rented?

5. A blueprint for a cottage has a scale of 1:40.

One room measures 3.4 m by 4.8 m.

Calculate the dimensions of the room on the blueprint.

6. For a painting, the ratio of the length to the width is 5:3.

The painting is 45 cm wide.

How long is the painting?

7. The ratio of the number of students who take trumpet lessons to clarinet lessons is 6:5.

The ratio of the number of students who take piano lessons to trumpet lessons is 8:3.

Ten students take clarinet lessons.

- a) How many students take trumpet lessons?
- **b)** How many students take piano lessons?
- **8.** The scale on a map is 1 cm represents 40 km.

The actual straight line distance between 2 cities is about 340 km.

What is the map distance between these 2 cities?

Lesson 5.9: Exploring Rates

- 1. Express each unit rate using symbols.
 - a) Gunther read 3 books in 1 day.
 - **b)** Coleen ran 12 km in 1 h.
 - c) Philip did 15 push-ups in 1 min.
 - **d**) Izzie paid \$2.95 for 1 kg of beans.
- 2. Express as a unit rate.
 - a) The bus travelled 80 km in 2 h.
 - **b)** Marco's heart beats 35 times in 30 s.
 - c) Inga walked 12 km in 4 h.
 - **d)** Wally washed 20 plates in 4 min.
 - e) Cherie delivered 150 catalogues in 2.5 h.

3. Sal earns \$24 in 3 h.

Josh earns \$13 in 2 h.

Komal earns \$44 in 4 h.

- a) Who makes the most money per hour?
- **b)** How much will the person who earns the most money per hour earn in 8 h?
- **4.** Fran bought 3 cans of soup for \$1.45. At this rate, how much will 6 cans cost?
- **5.** James read 48 pages in 90 min. How many pages could he read in 5 h?
- **6. a)** A car travels at an average speed of 50 km/h. How long will it take to travel 200 km?
 - **b)** A car travels at an average speed of 40 km/h. Will it take more or less time to travel 200 km?
- **7.** Write each speed in metres per second.
 - a) A river otter swims at about 10 km/h.
 - **b)** An ostrich can run at about 51 km/h.
- **8.** A 300-g package of pepperoni costs \$4.29.
 - a) What is the cost per 100 g?
 - **b)** How much would 1 kg cost?
 - c) How much pepperoni could you buy with \$20?

Lesson 5.10: Comparing Rates

- 1. Write a unit rate for each statement.
 - a) 560 km travelled in 7 h
 - **b)** 4 cans of beans for \$1.76
 - c) 280 words typed in 7 min
 - **d)** \$786 earned in 6 weeks
- 2. Banana chips sell for 44¢ per 100 g. How much would 450 g of banana chips cost?
- **3.** Which is the greatest average speed?
 - a) 78 km in 3 h
 - **b)** 96 km in 4 h
 - c) 125 km in 5 h

- **4.** Which is the better buy?
 - **a)** 5 oranges for \$1.65 or 8 oranges for \$2.77
 - **b)** 2 L of lemonade for \$2.56 or 1 L for \$1.32
 - **c)** 3 kg of apples for \$5.70 or 2 kg for \$3.90
- **5.** A 2.5-kg bag of flour contains enough flour to make 4 cakes.
 - a) How much flour is needed to make 50 cakes?
 - **b)** How many bags of flour do you need?
- **6.** Ned types 360 words in 6 min.

Nate types 220 words in 4 min.

Who would type more words in 10 min?

What assumptions do you make?

- 7. In the first 8 games of the hockey season, Moira scored 26 goals.
 - a) On average, how many goals did Moira score per game?
 - **b)** At this rate, how many goals will Moira score in 20 games?
- **8.** The courier travelled 508 km in 8 h.
 - a) What was the average speed?
 - **b)** At this rate, how long will it take the courier to travel 889 km?
- **9.** Benny's cat will eat 2 different brands of cat food. Brand A costs \$6.99 for a 1.3-kg bag. Brand B costs \$16.99 for a 4.5-kg bag.
 - **a)** Find the unit cost of each brand of cat food. Which brand is the better buy?
 - **b)** Why might Benny not buy the brand in part a?